

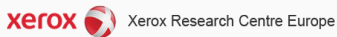
# DECODING DISTRIBUTED TREE STRUCTURES

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<sup>1</sup>University of Rome “Tor Vergata”

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# INTRODUCTION

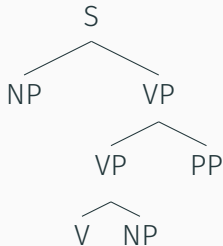
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- Natural language processing tasks benefit from syntactic information

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## Directly

- Symbolic Tree Structures

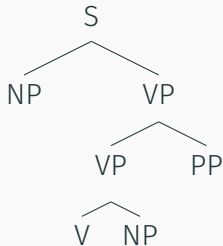


- Tree Kernels (Collins; 2001)

- Natural language processing tasks benefit from syntactic information

## Directly

- Symbolic Tree Structures



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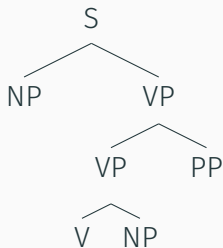
## Indirectly

- Distributed Tree Structures

- Natural language processing tasks benefit from syntactic information

## Directly

- Symbolic Tree Structures



- Tree Kernels (Collins; 2001)

## Indirectly

- Distributed Tree Structures

$$\longrightarrow \mathbf{t} = (0.0112, 0.212, \dots, 0.0081) \in \mathbb{R}^d$$

## Distributed Trees (Zanzotto; 2012)

- Approximate tree kernels (Collins; 2001)

$$\langle \mathbf{t}_1, \mathbf{t}_2 \rangle \approx TK(T_1, T_2)$$

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- Faster to compute than tree kernels



## Distributed Trees (Zanzotto; 2012)

- Approximate tree kernels (Collins; 2001)

$$\langle \mathbf{t}_1, \mathbf{t}_2 \rangle \approx TK(T_1, T_2)$$

- Faster to compute than tree kernels
- Can be used as input in any algorithm
  - Neural network
  - Support Vector Machines
  - ...

## WHAT'S IN A DISTRIBUTED VECTORS?

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## Question

- How much information is stored in a distributed vector?
- In other words, can we decode the structured representation from a distributed vector?

## Our Idea

- Traditional parsing:
  - CYK algorithm (and others)
- Use distributed vectors to “*guide*” the algorithm choices

## CYK (Cocke, Younger, Kasami; 1967)

Given a sentence  $s$  of length  $n$  and a grammar  $G$ :

- builds a  $n \times n$  table which contains the partial parses of the sentence

## Grammar:

$S \rightarrow NP VP$

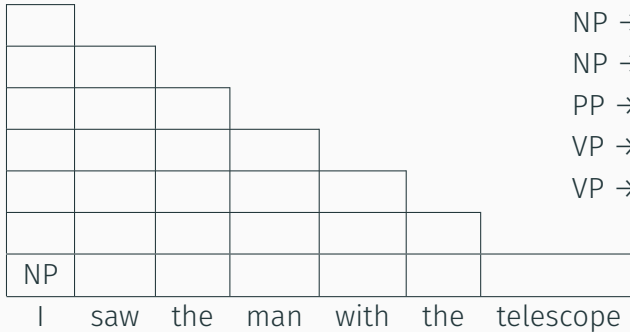
$NP \rightarrow DET N$

$NP \rightarrow NP PP$

$PP \rightarrow P NP$

$VP \rightarrow V NP$

$VP \rightarrow VP PP$



## Grammar:

$S \rightarrow NP VP$

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$NP \rightarrow NP PP$

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$VP \rightarrow V NP$

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NP	V						
I	saw	the	man	with	the	telescope	

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$PP \rightarrow P NP$

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NP	V	DET					
I	saw	the	man	with	the	telescope	



## Grammar:

$S \rightarrow NP VP$

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$NP \rightarrow NP PP$

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NP	V	DET	N				
I	saw	the	man	with	the	telescope	

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$VP \rightarrow VP PP$

NP	V	DET	N	P			
I	saw	the	man	with	the	telescope	

## Grammar:

$S \rightarrow NP VP$

$NP \rightarrow DET N$

$NP \rightarrow NP PP$

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NP	V	DET	N	P	DET		
I	saw	the	man	with	the	telescope	

## Grammar:

$S \rightarrow NP VP$

$NP \rightarrow DET N$

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NP	V	DET	N	P	DET	N	
I	saw	the	man	with	the	telescope	

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.						
NP	V	DET	N	P	DET	N
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	.					
NP	V	DET	N	P	DET	N
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		.				
NP	V	DET	N	P	DET	N
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		NP				
NP	V	DET	N	P	DET	N
I	saw	the	man	with	the	telescope

## Grammar:

$S \rightarrow NP VP$

$NP \rightarrow DET N$

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We also store  
backpointers to  
record what rule  
we choose

		NP				
NP	V	DET	N	P	DET	N
I	saw	the	man	with	the	telescope

## Grammar:

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		NP	.			
NP	V	DET	N	P	DET	N
I	saw	the	man	with	the	telescope

		NP		.		
NP	V	DET	N	P	DET	N
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		NP			NP	
NP	V	DET	N	P	DET	N
I	saw	the	man	with	the	telescope

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		NP			NP	
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	VP					
		NP			NP	
NP	V	DET	N	P	DET	N
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	VP	.				
		NP			NP	
NP	V	DET	N	P	DET	N
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		NP			NP	
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	VP			PP		
		NP			NP	
NP	V	DET	N	P	DET	N
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S						
	VP			PP		
		NP			NP	
NP	V	DET	N	P	DET	N
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S	.					
	VP			PP		
		NP			NP	
NP	V	DET	N	P	DET	N
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S		.				
	VP			PP		
		NP			NP	
NP	V	DET	N	P	DET	N
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S			.			
	VP			PP		
		NP			NP	
NP	V	DET	N	P	DET	N
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.						
S						
	VP			PP		
		NP			NP	
NP	V	DET	N	P	DET	N
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	.					
S						
	VP			PP		
		NP			NP	
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		NP				
S						
	VP			PP		
		NP			NP	
NP	V	DET	N	P	DET	N
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.						
		NP				
S						
	VP			PP		
		NP			NP	
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	.					
		NP				
S						
	VP			PP		
		NP			NP	
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	VP					
		NP				
S						
	VP			PP		
		NP			NP	
NP	V	DET	N	P	DET	N
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$VP \rightarrow V NP$

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	VP, VP					
		NP				
S						
	VP			PP		
		NP			NP	
NP	V	DET	N	P	DET	N
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Again, we store  
backpointers for  
the two  
possibilities

	VP, VP					
		NP				
S						
	VP			PP		
		NP			NP	
NP	V	DET	N	P	DET	N
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S							
	VP, VP						
		NP					
S							
	VP			PP			
		NP			NP		
NP	V	DET	N	P	DET	N	
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- Even in this small example there are two plausible interpretations



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- Even in this small example there are two plausible interpretations
- In general there are (exponentially) many more!
- Usually parsers use probabilistic grammars to disambiguate
  - Each rule of the grammar has an inherent probability (which must be learned)

## Idea

We show that a reference distributed vector of the correct parse is enough to eliminate ambiguity

(and thus reconstruct the original parse)

Ingredients:

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- Reference grammar  $G$

## Grammar:

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### Ingredients:

- Reference grammar  $G$
- Distributed vector  $\mathbf{t}$

### Grammar:

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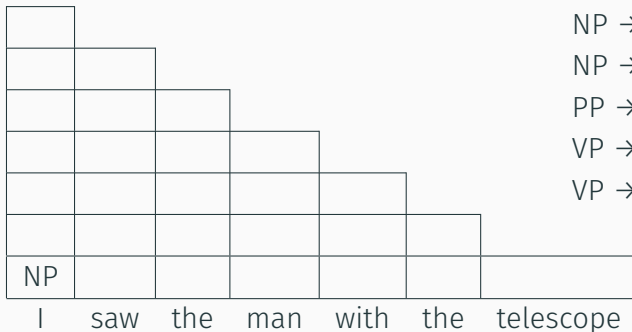
$PP \rightarrow P NP$

$VP \rightarrow V NP$

$VP \rightarrow VP PP$

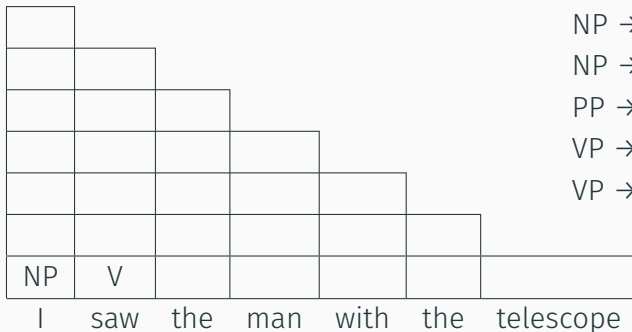
$$t \rightarrow \mathbf{t} = (0.011, 0.212, \dots, 0.008) \in \mathbb{R}^d$$

## Grammar:

 $S \rightarrow NP VP$  $NP \rightarrow DET N$  $NP \rightarrow NP PP$  $PP \rightarrow P NP$  $VP \rightarrow V NP$  $VP \rightarrow VP PP$ 

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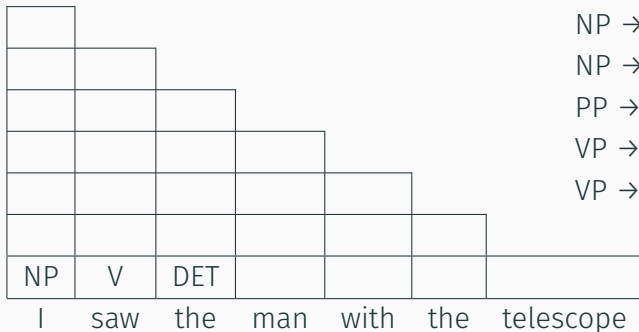
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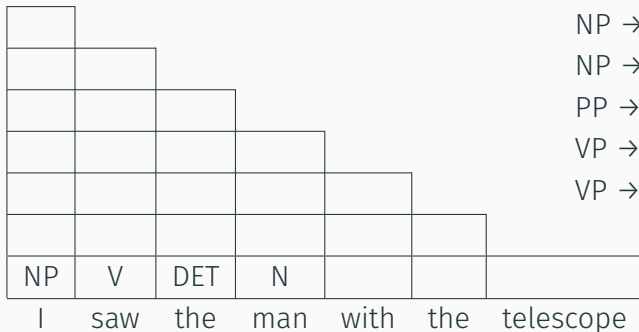
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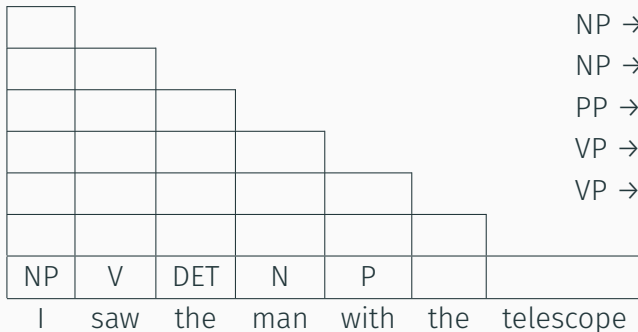
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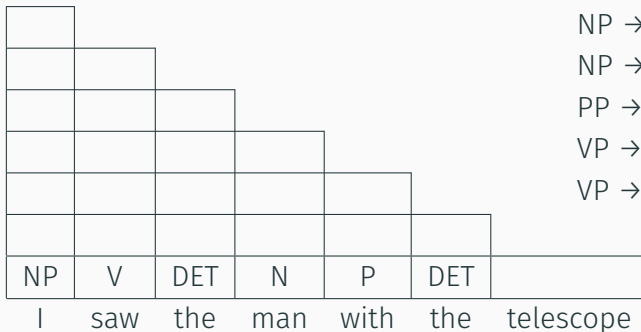
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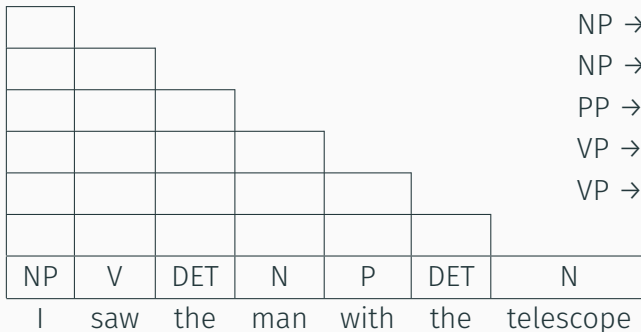
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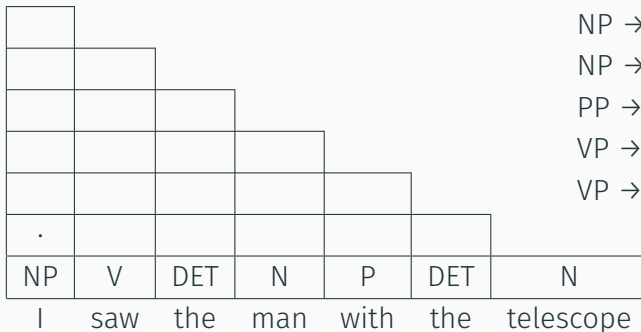
$$t \rightarrow \mathbf{t} = (0.011, 0.212, \dots, 0.008) \in \mathbb{R}^d$$

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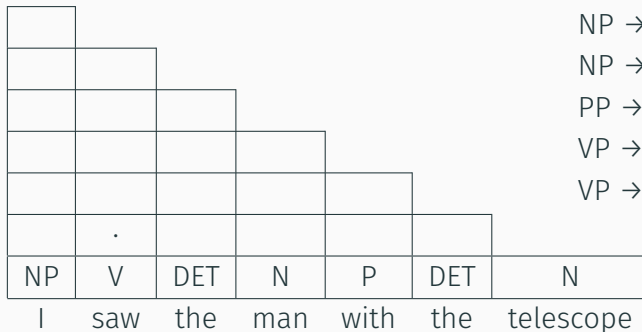
$$t \rightarrow \mathbf{t} = (0.011, 0.212, \dots, 0.008) \in \mathbb{R}^d$$

## Grammar:

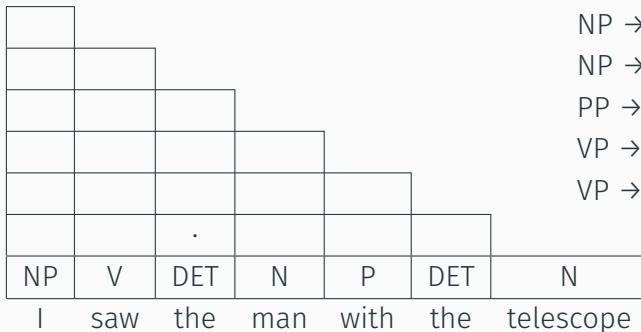
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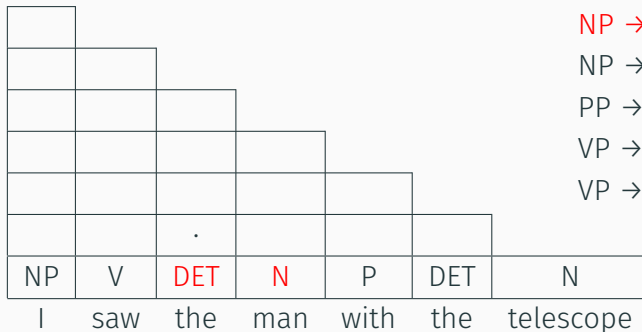
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**Grammar:** $S \rightarrow NP VP$  $NP \rightarrow DET N$  $NP \rightarrow NP PP$  $PP \rightarrow P NP$  $VP \rightarrow V NP$  $VP \rightarrow VP PP$ 

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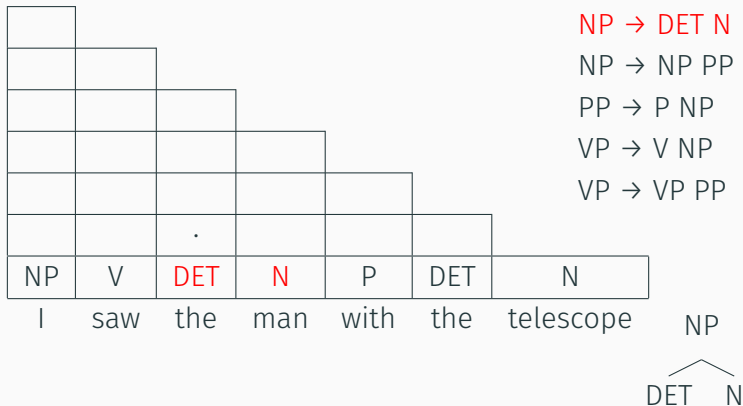


Grammar:

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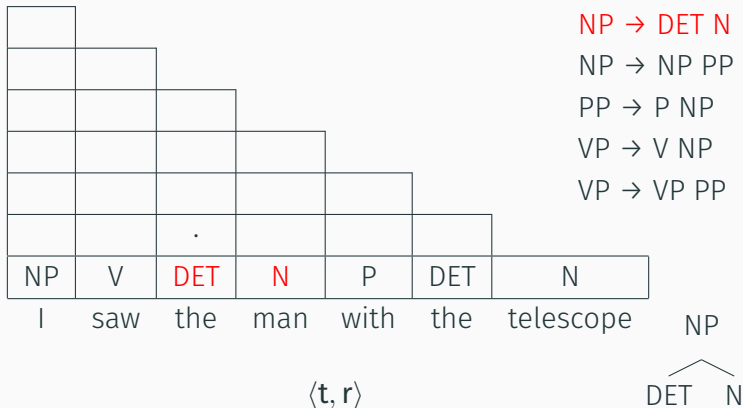
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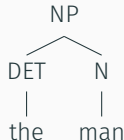
$$\mathbf{t} \rightarrow \mathbf{t} = (0.011, 0.212, \dots, 0.008) \in \mathbb{R}^d \quad \mathbf{r} = (0.005, 0.043, \dots, 0.016)$$

Grammar:

 $S \rightarrow NP VP$  $NP \rightarrow DET N$  $NP \rightarrow NP PP$  $PP \rightarrow P NP$  $VP \rightarrow V NP$  $VP \rightarrow VP PP$ 

$$\mathbf{t} \rightarrow \mathbf{t} = (0.011, 0.212, \dots, 0.008) \in \mathbb{R}^d \quad \mathbf{r} = (0.005, 0.043, \dots, 0.016)$$

We store the full subtrees here!



**Grammar:**

$S \rightarrow NP VP$

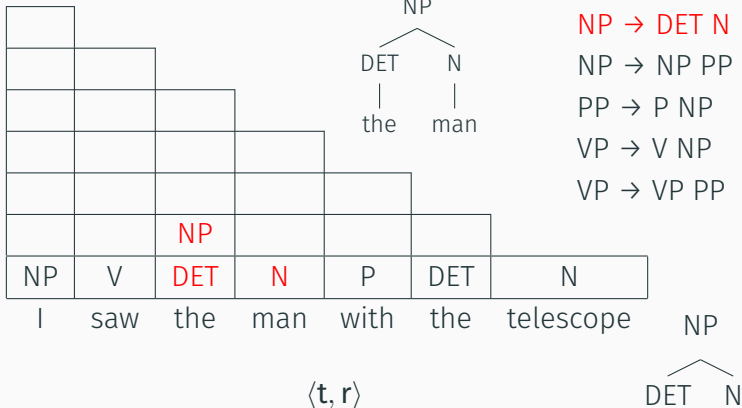
$NP \rightarrow DET N$

$NP \rightarrow NP PP$

$PP \rightarrow P NP$

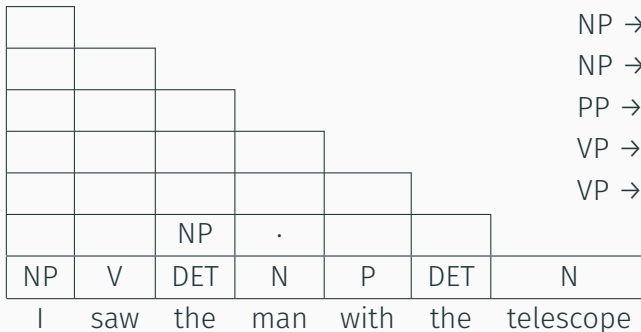
$VP \rightarrow V NP$

$VP \rightarrow VP PP$



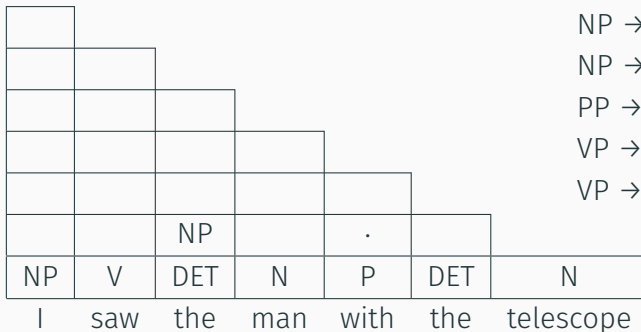
$$t \rightarrow \mathbf{t} = (0.011, 0.212, \dots, 0.008) \in \mathbb{R}^d \quad \mathbf{r} = (0.005, 0.043, \dots, 0.016)$$

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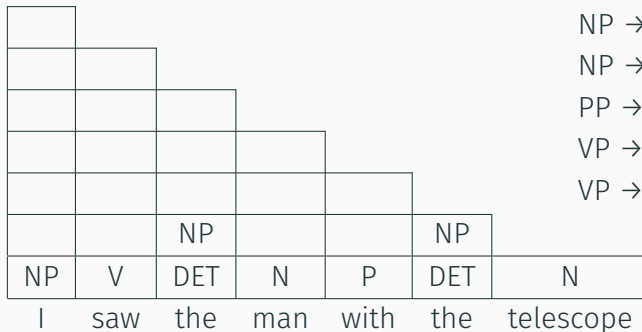
$$t \rightarrow \mathbf{t} = (0.011, 0.212, \dots, 0.008) \in \mathbb{R}^d$$

## Grammar:

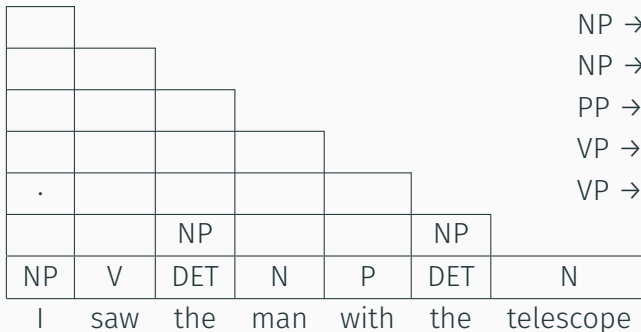
 $S \rightarrow NP VP$  $NP \rightarrow DET N$  $NP \rightarrow NP PP$  $PP \rightarrow P NP$  $VP \rightarrow V NP$  $VP \rightarrow VP PP$ 

$$t \rightarrow \mathbf{t} = (0.011, 0.212, \dots, 0.008) \in \mathbb{R}^d$$

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NP	V	DET	N	P	DET	N	
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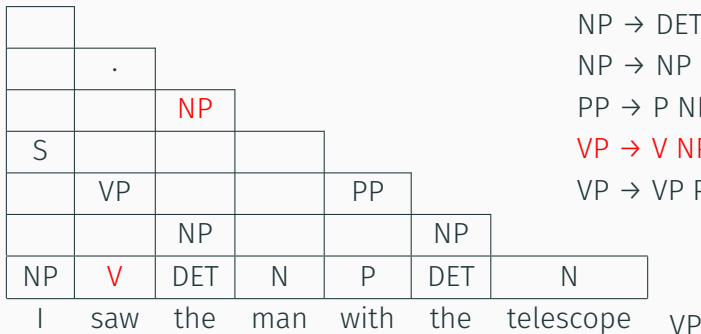
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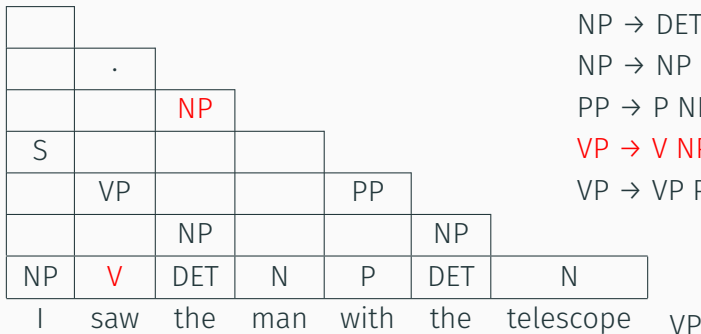
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$\langle \mathbf{t}, \mathbf{r}_1 \rangle$

$\begin{array}{c} \wedge \\ V \quad NP \end{array}$

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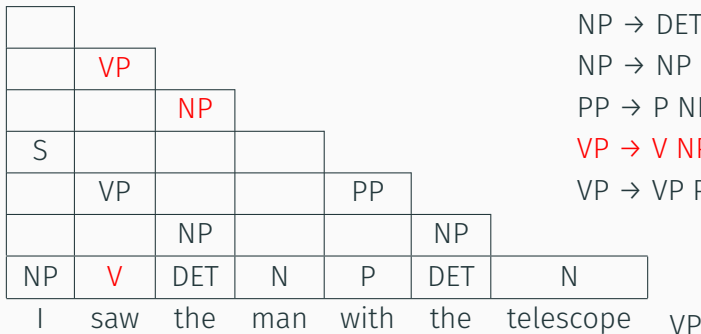
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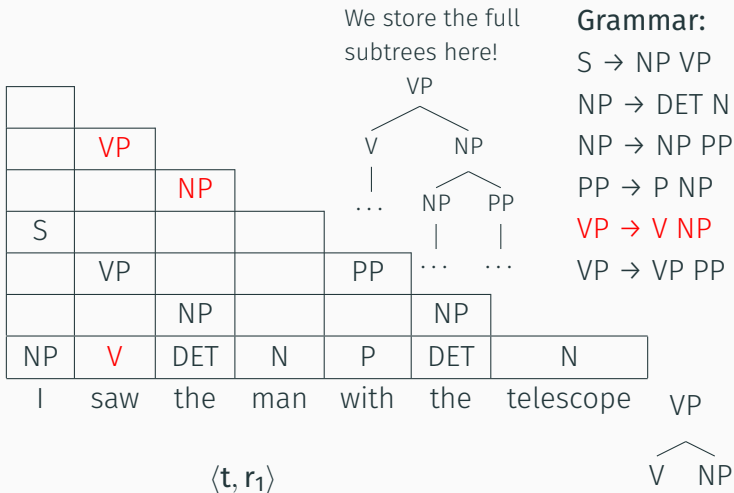


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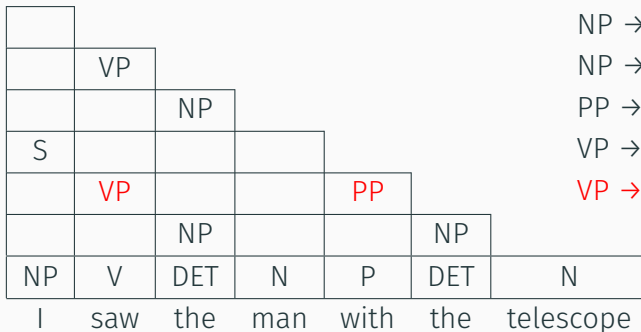
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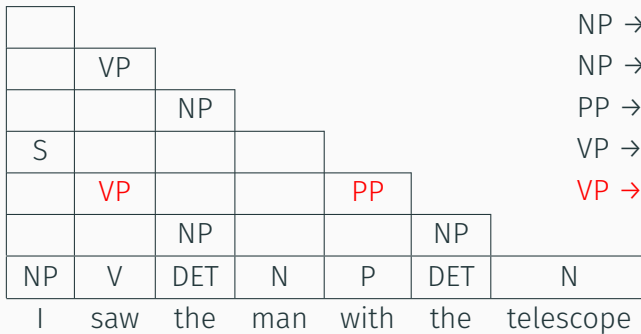
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## Grammar:

$S \rightarrow NP VP$

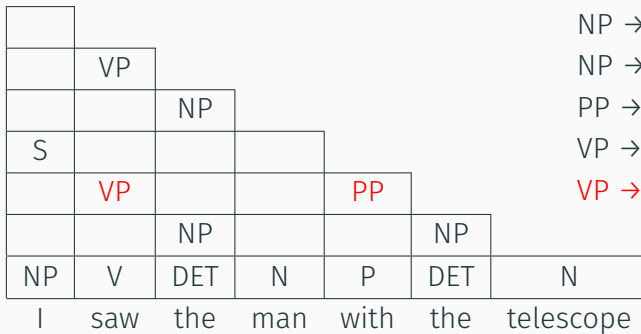
$NP \rightarrow DET N$

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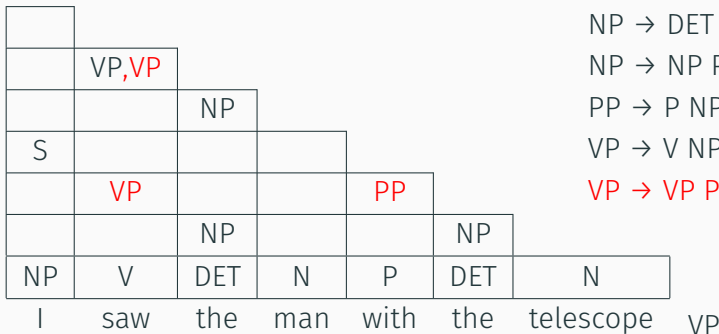


$\langle \mathbf{t}, \mathbf{r}_2 \rangle$



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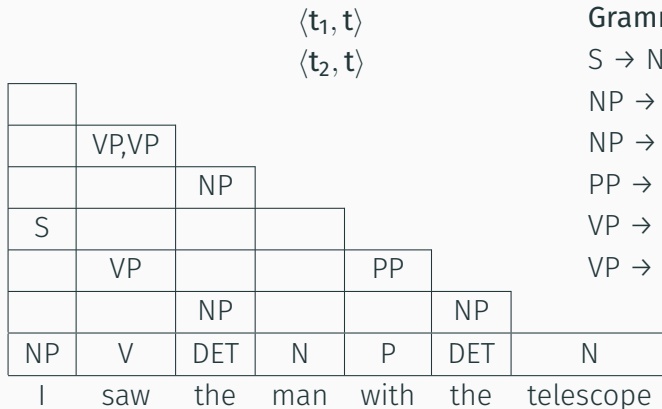
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$\begin{array}{c} \diagup \quad \diagdown \\ VP \quad PP \end{array}$

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	VP,VP						
		NP					
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## EXPERIMENTS AND RESULTS

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## Dataset

Wall Street Journal sections of PennTree Bank:

- Sections 1~23: Grammar extraction
- Section 24: testing

## Experimental pipeline

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  - compare the result with the correct tree



## Parameters

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- $d$ : Dimension of the vector representation

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- $k$ : number of partial trees kept in each cell
  - we only report  $k = 2$

## Results

- Number of exactly reconstructed trees;
- (Labelled) precision, recall and f-measure;

1024	2048	4096	8192	16384
23.5%	52.32%	75.58%	87.5%	<b>92.79%</b>

**Table 1:** Percentage of exactly reconstructed sentence

	1024	2048	4096	8192	16384
<i>precision</i>	0.71	0.85	0.951	0.99	<b>0.994</b>
<i>recall</i>	0.477	0.78	0.929	0.967	<b>0.976</b>
<i>f-measure</i>	0.57	0.81	0.939	0.974	<b>0.984</b>

**Table 2:** Precision, recall and F-measure

## SUMMARY AND FUTURE WORK

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- Use the reconstruction method on other distributed representations

QUESTIONS?